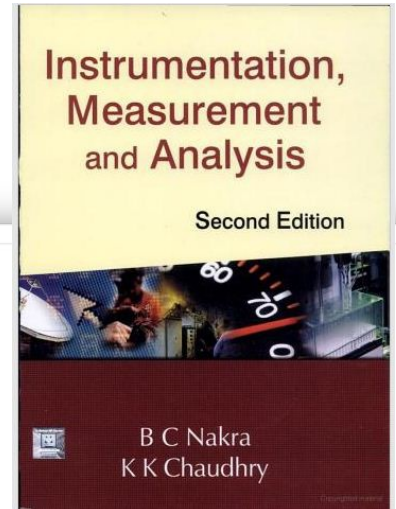


**B.Sc. (Semester - 6)**  
**Subject: Physics**  
**Course: US06CPHY06**  
**Instrumentation and Sensors**  
**(Three Credit Course –3 Hours per week)**  
**(Effective from June-2012)**

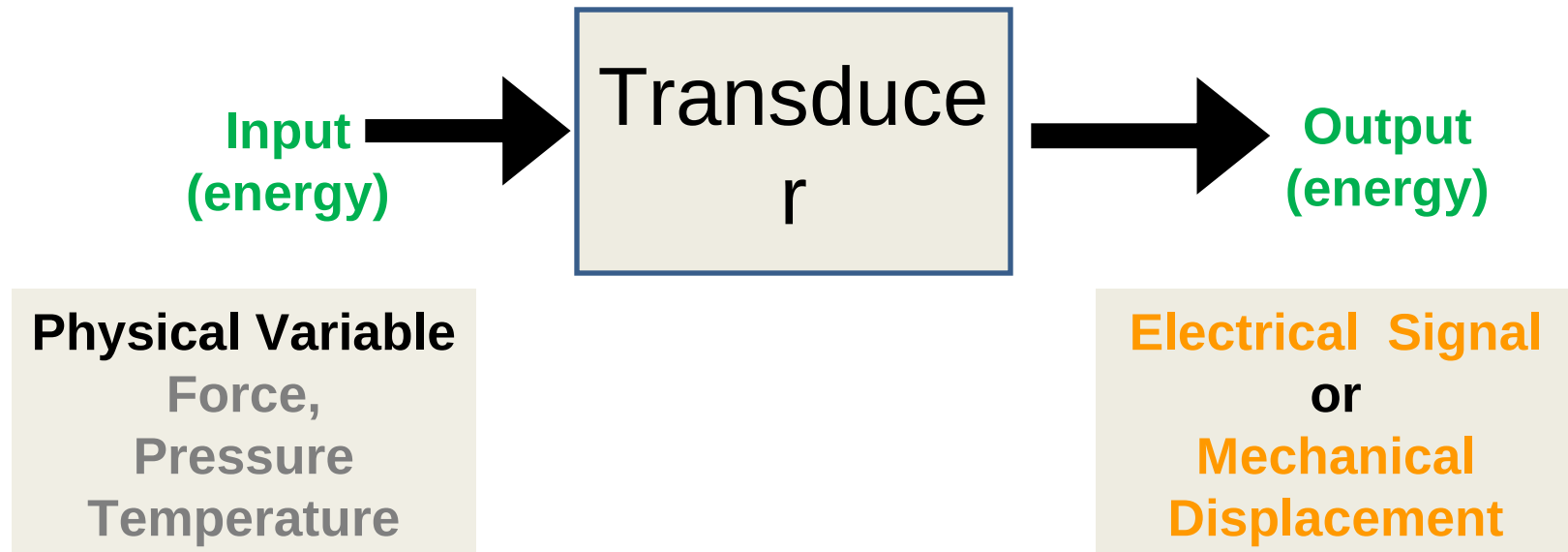


**UNIT – I      CRO and Transducer Elements**

Introduction to Cathode Ray Oscilloscope, Cathode Ray Tube, Deflection system in CRT, Analog Transducers, Electromechanical Type Transducer, Potentiometric resistance type, Inductive Type, Capacitive Type, Piezo-Electric Transducer, Dynamic Characteristics of Piezo-Electric Transducers, Resistance Strain Gauges, Unbounded Strain Gauge, Bonded Strain Gauge, Resistance Strain Gauge Bridges, Balanced Bridge, Unbalanced Bridge

# What is a Transducer ?

## Principle of Working:



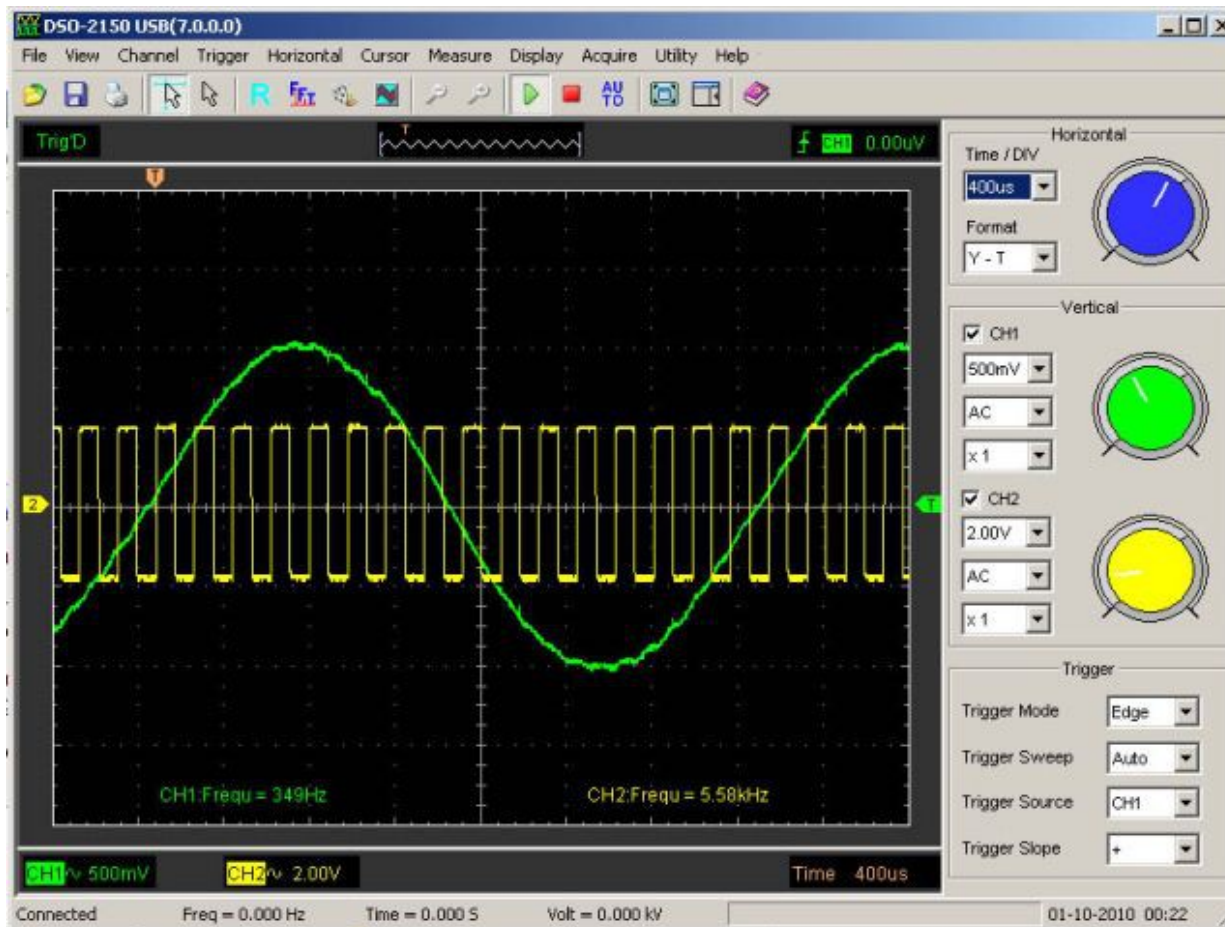
Advantage of electrical signal at the output:

1. Inertia and friction effects are absent, unlike in transducers with mechanical outputs.
2. Amplification can be obtained with relative ease.
3. Indication or recording, especially at a distance, is greatly facilitated.

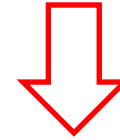
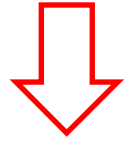
# Transducers Types: Classification

**Analog** : With variations of input, output changes continuously.

**Digital** : With variations of input, output changes non-continuously i.e. In a discrete manner.



# Analog Transducers



## **Electro-Mechanical Transducers:**

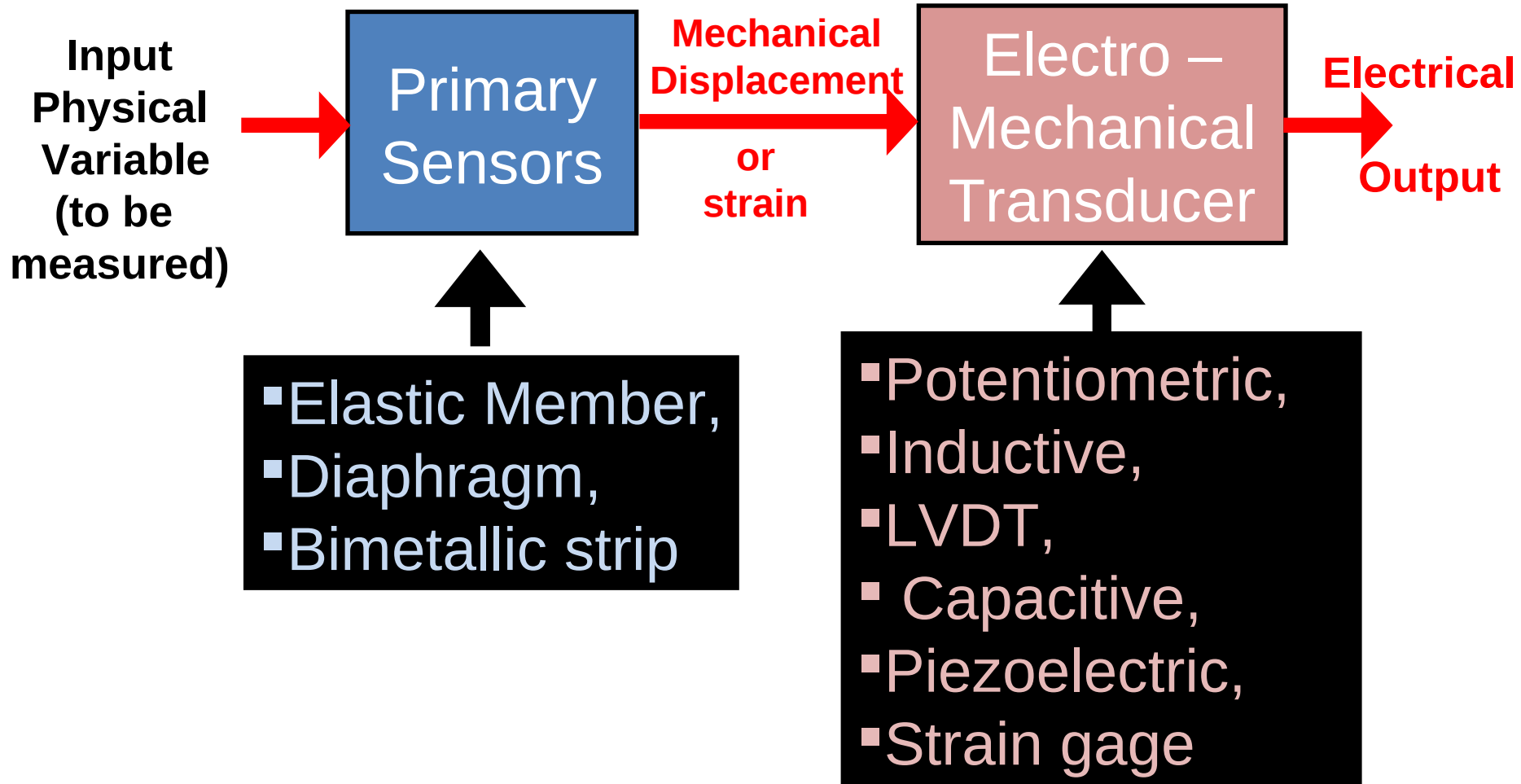
1. Potentiometric Resistance Type
2. Inductance Type
3. Capacitance Type
4. Piezo-electric Type
5. Resistance Strain Gages
6. Ionization Type
7. Mechano-Electrical Type

## **Opto-Electrical Transducers:**

1. Photo-emissive Type
2. Photo-conductive Type
3. Photo-voltaic Type.

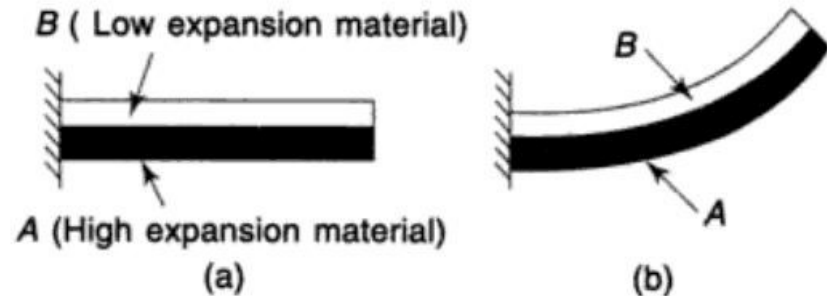
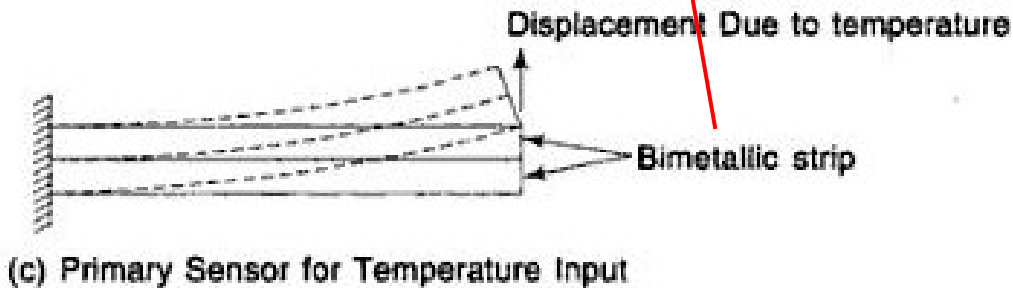
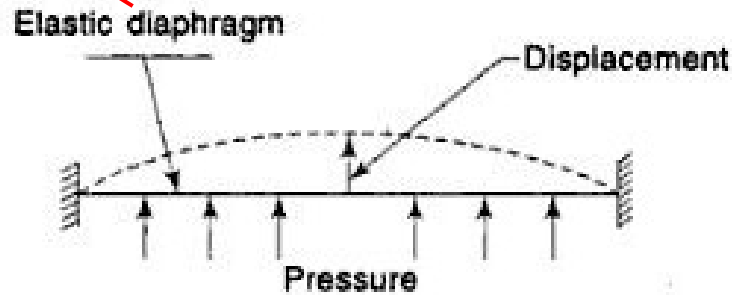
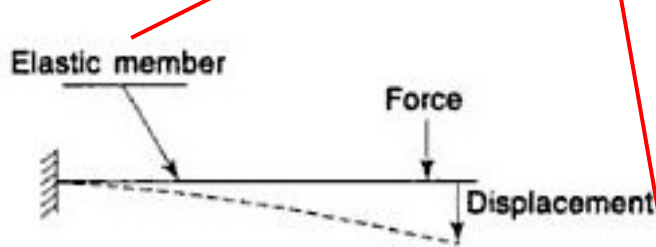
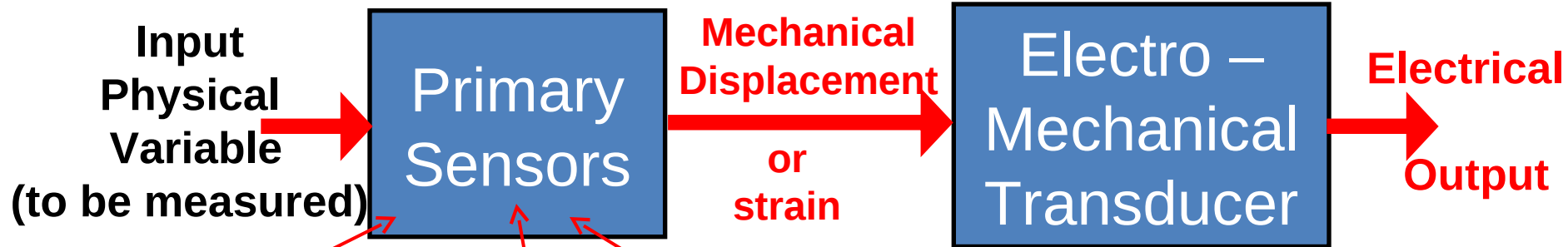
# Electromechanical Transducers

## Principle of Measurements



# Electromechanical Transducers

## Primary Sensors for Displacements



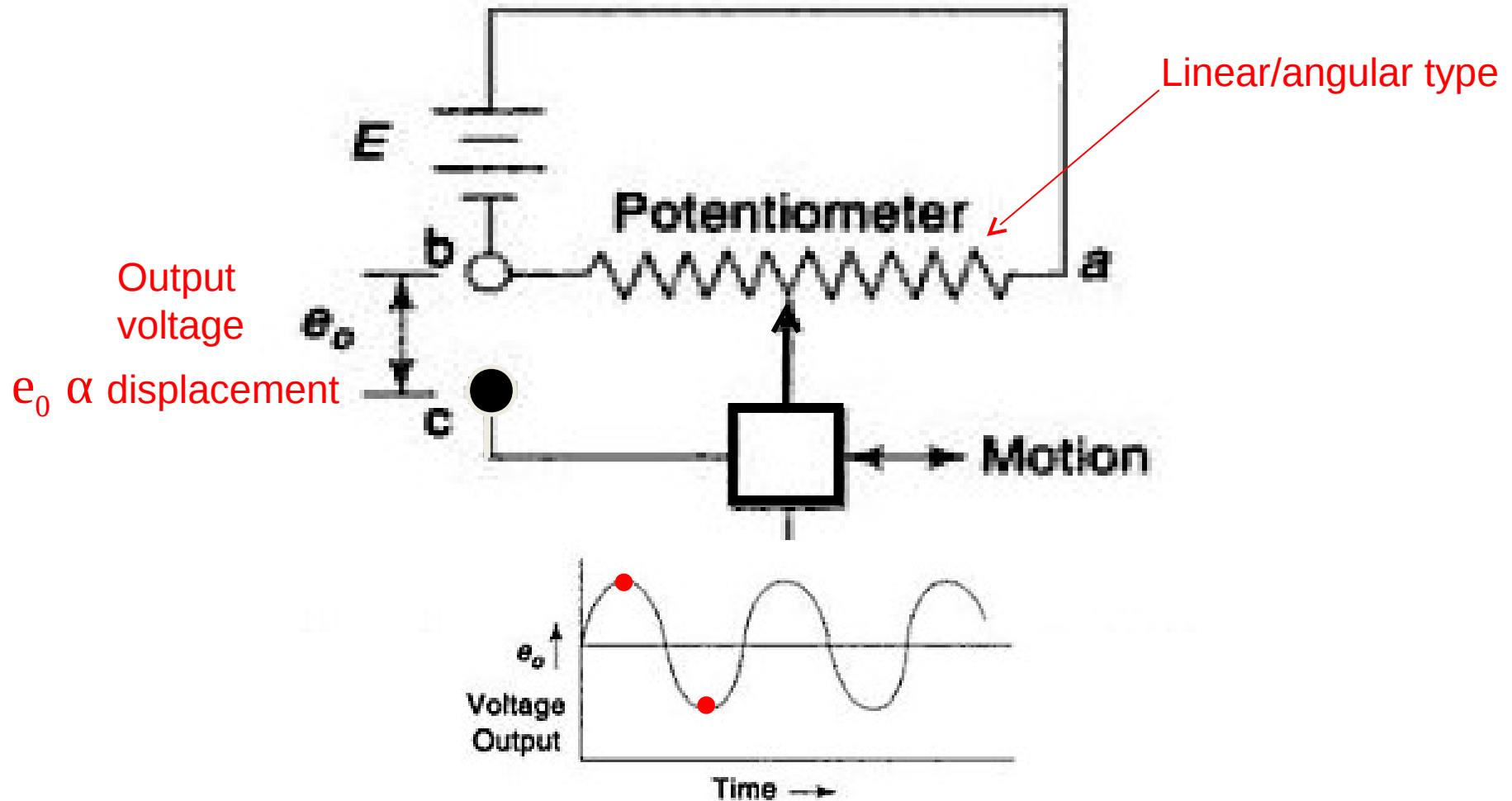
## Selection criterion for Motion Transducers:

Since displacement or motion is input to an EMT, they are called as

*“Motion Transducers”*

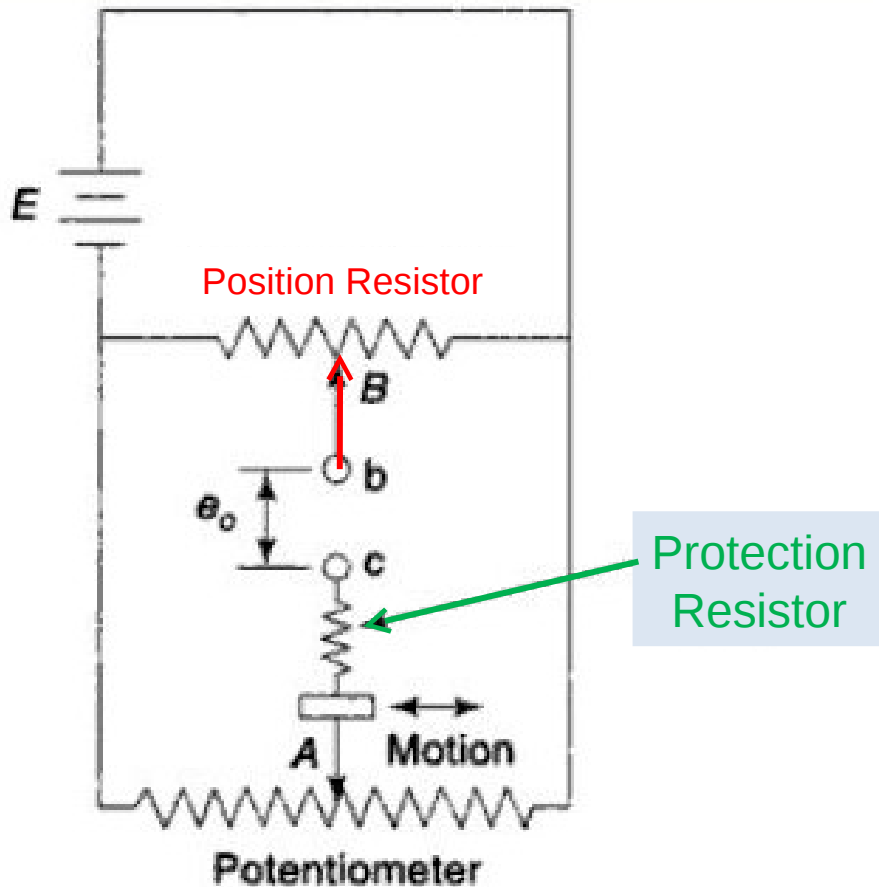
1. Magnitude of Motion: small/medium/ large?
2. Input-Output Relation: to displacement  $x$  /  $(dx/dt)$  /  $(d^2x/dt^2)$ ?
3. Static / Dynamic Characteristics: of motion to be measured.
4. Attachment / Proximity Type: to moving object
5. Self-generating / external source type: to energies the Trans.
6. Type of Associated Circuit: Simple or complicated.

# Potentiometric Resistance Transducers





# Modified Potentiometric Resistance Transducers



**Position resistor** at  $B$  is used to bring the initial value of  $e_0$  to zero depending on the initial position of the moving point.

In case when the resistors are so placed that there is a short circuit across the battery, the movable contacts of the potentiometer may burn off. A **Protection Resistor** as shown in figure prevents this.

# Inductive type Transducers

## Principle of Operation:

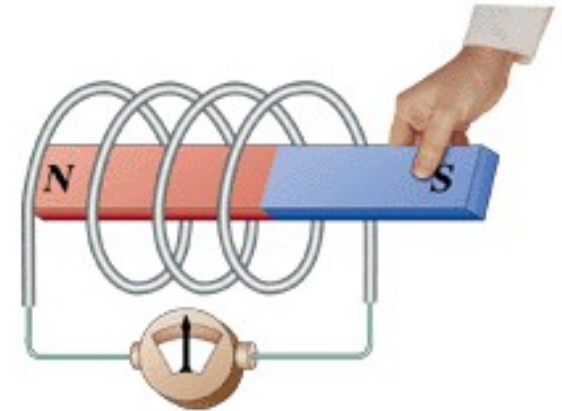
The magnetic characteristics of an electric circuit changes

due to the motion of the

### ▪ Self-generating type:

In which a *voltage signal is generated in the transducer due to the relative motion of conductor and a magnetic field.*

e.g. electrodynamic, electromagnetic and eddy current type inductive transducers



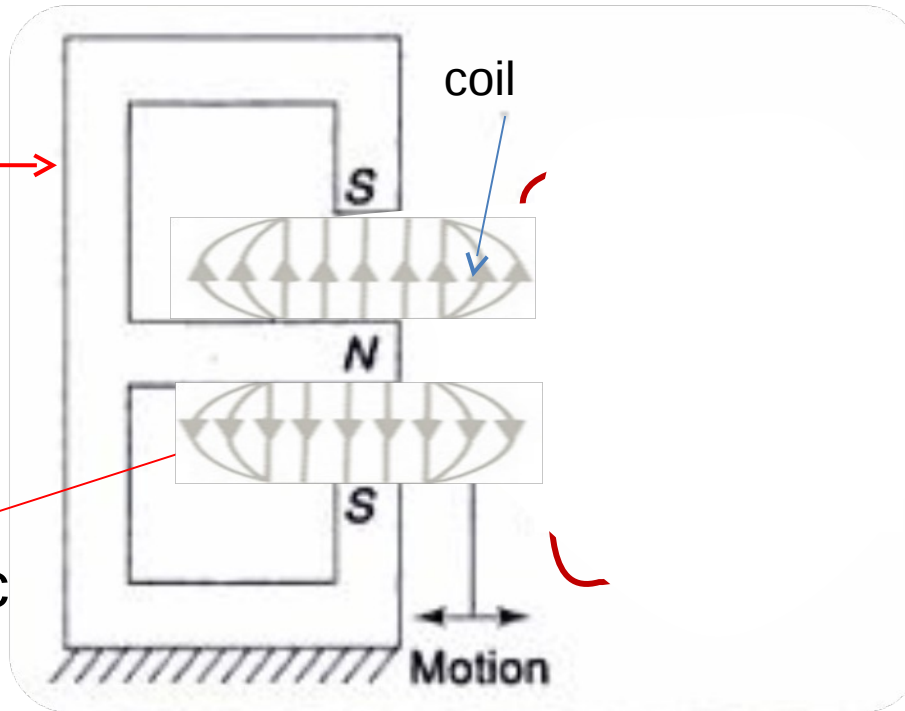
### ▪ Non-Self-generating type:

*External source is needed* to energize a coil/coils, the inductance of which would change due to the relative motion of conductor and a magnetic field.

# Electrodynamic - Linear Motion

Fixed Magnet

Non-Magnetic material



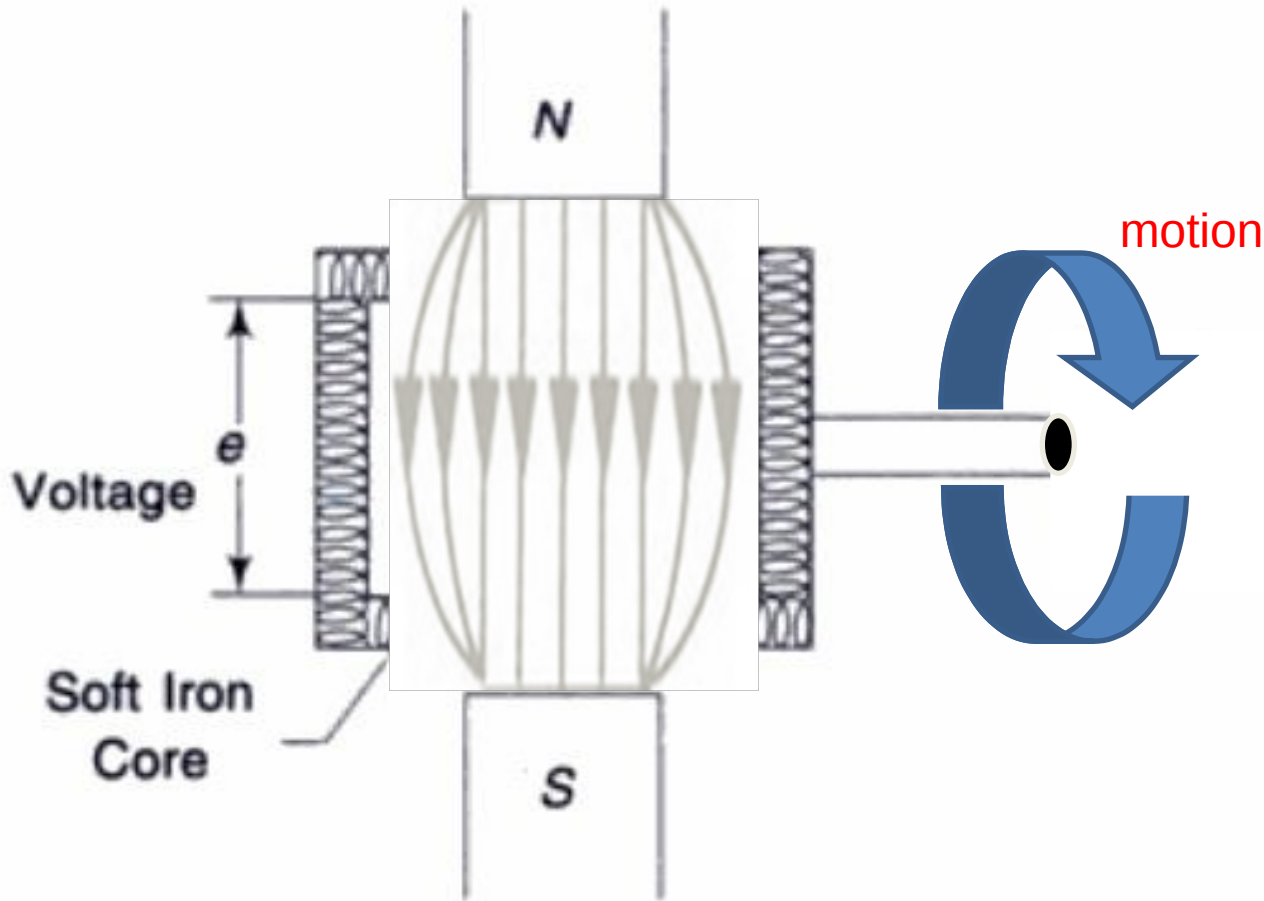
Change in magnetic flux

Induced voltage  
 $e \propto (d\phi/dt)$

i.e.  $e \propto (d^2x/dt^2)$

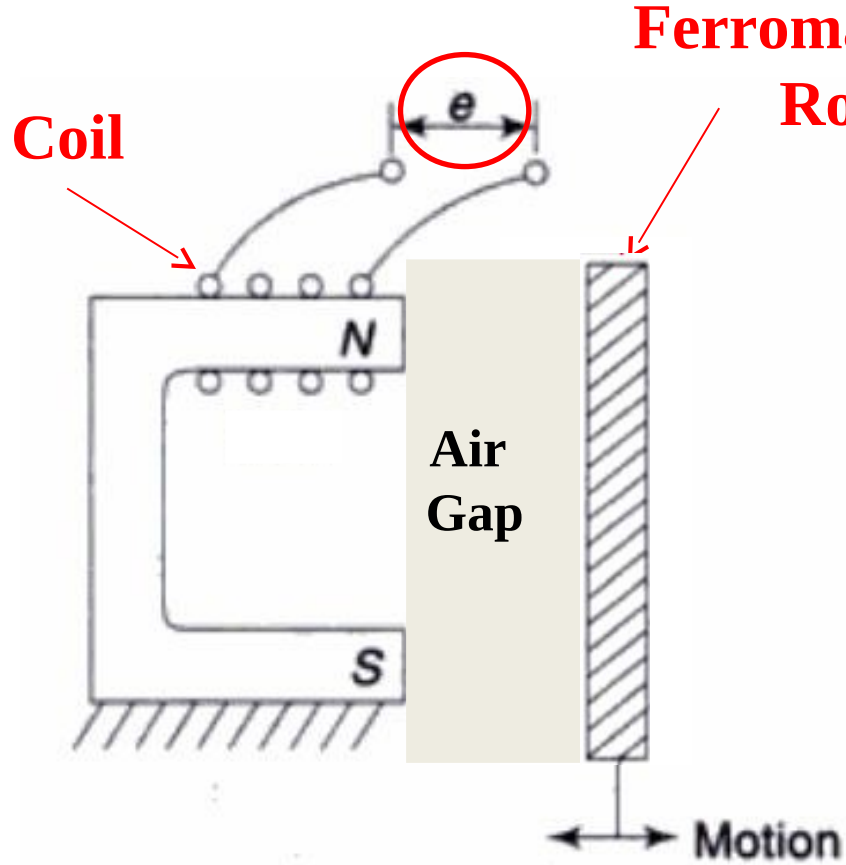
Attachment Type  
Velocity transducer

# Electrodynamic: Rotary Motion



- Change in magnetic flux
- Attachment Type
- Velocity transducer

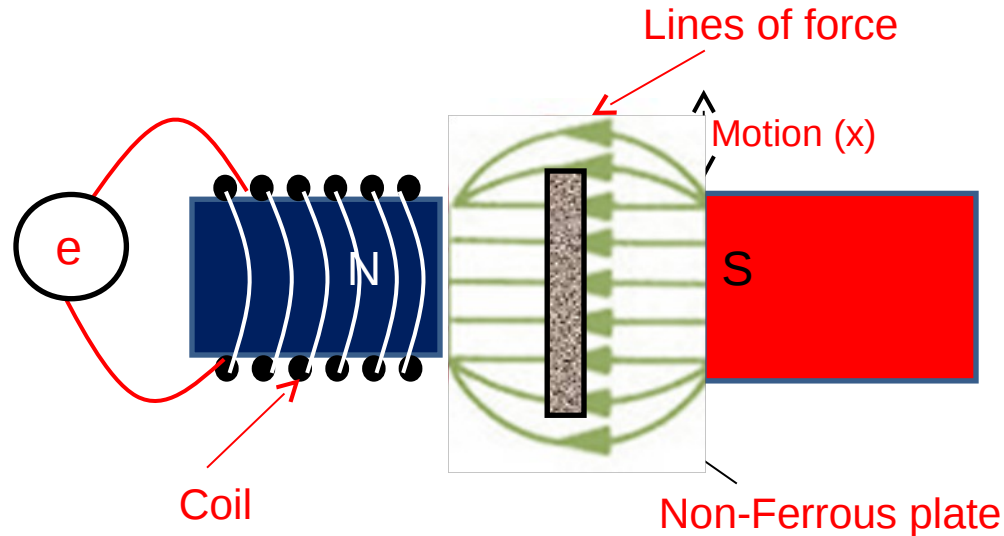
# Electromagnetic Type:



- Change in air gap
- Change in magnetic flux
- Induced voltage
- Proximity Type
- Velocity transducer

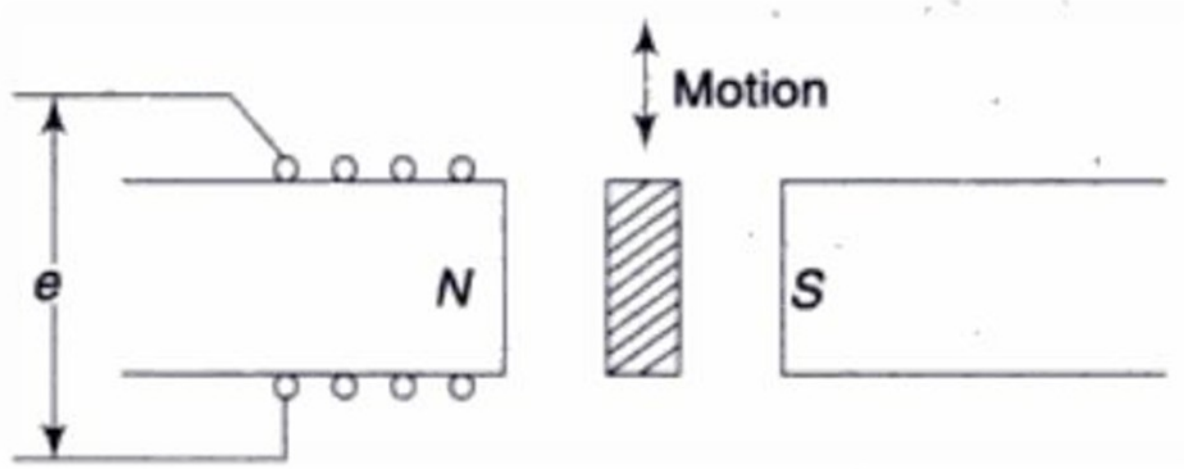
Limitation: linear for small motions

# Eddy Current Type:



- The motion generates Eddy current  $i$  in the plate, which set-up a **mag. field** in the direction opposing the **mag. field** that generated them.
- The output voltage,  $e \propto (di/dt)$  i.e.  $e \propto (d^2x/dt^2)$
- **linear characteristics since gap remains constant**

# Eddy Current Type:



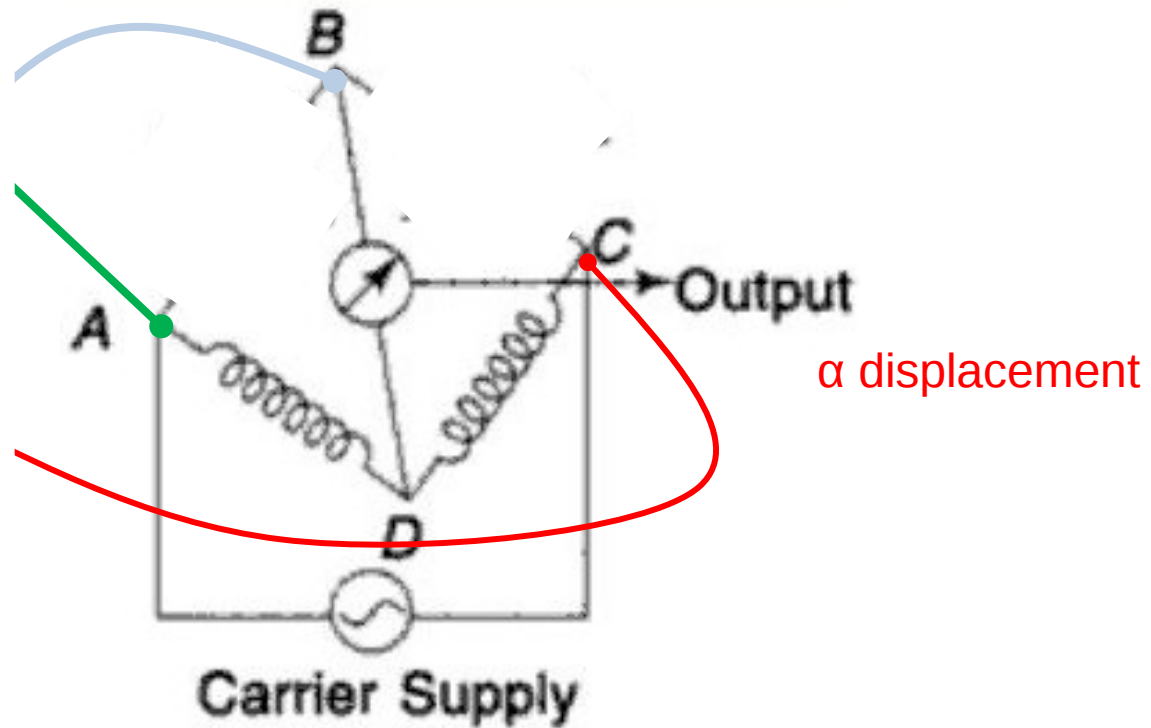
# Non-Self generating Inductive Type:

Non-Self-generating type:

**Principle:** External source is needed to energize a coil/coils, the inductance of which would change due to the relative motion of conductor and a magnetic field.

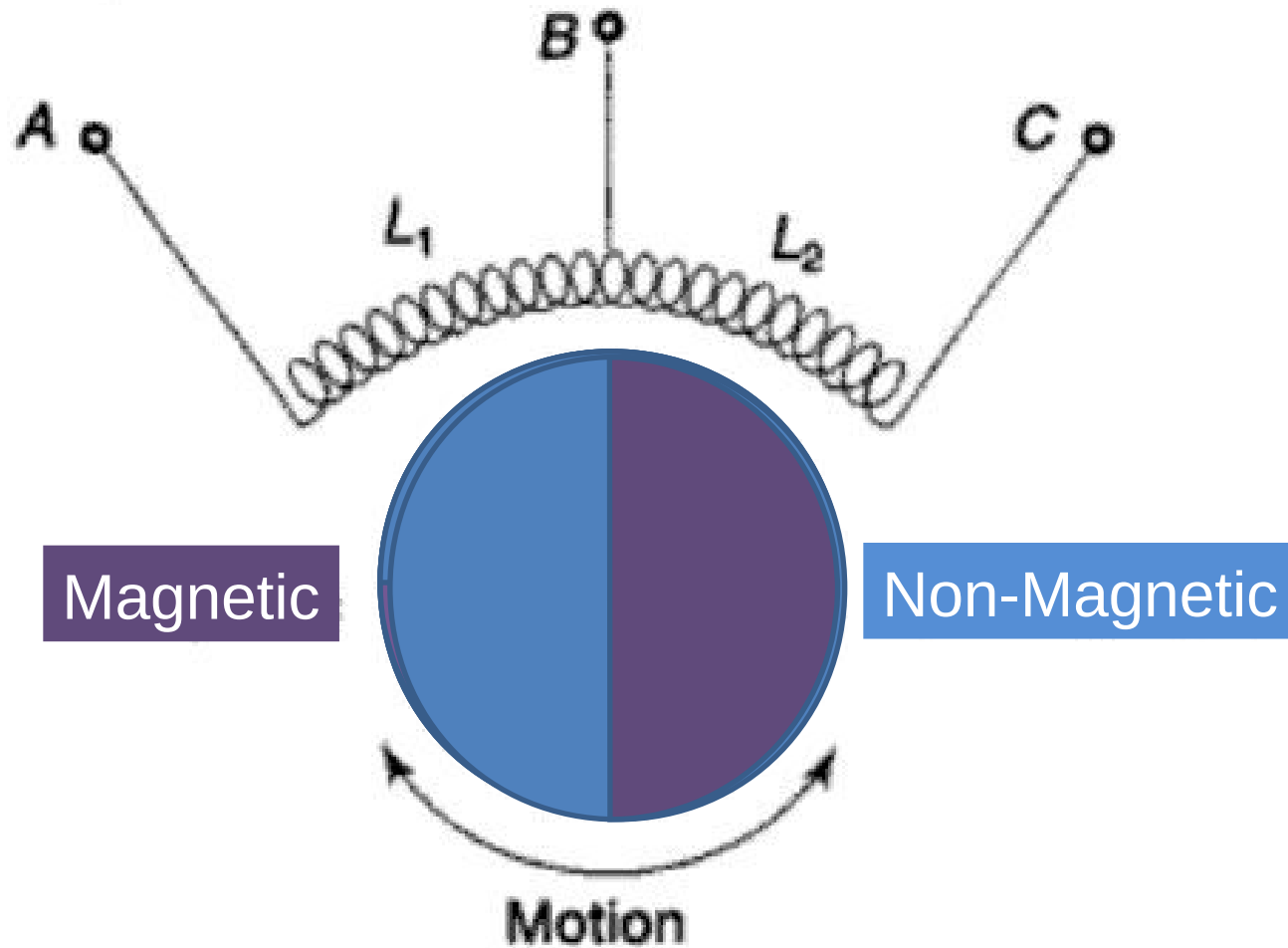


# Variable Inductance Type: Linear Motion

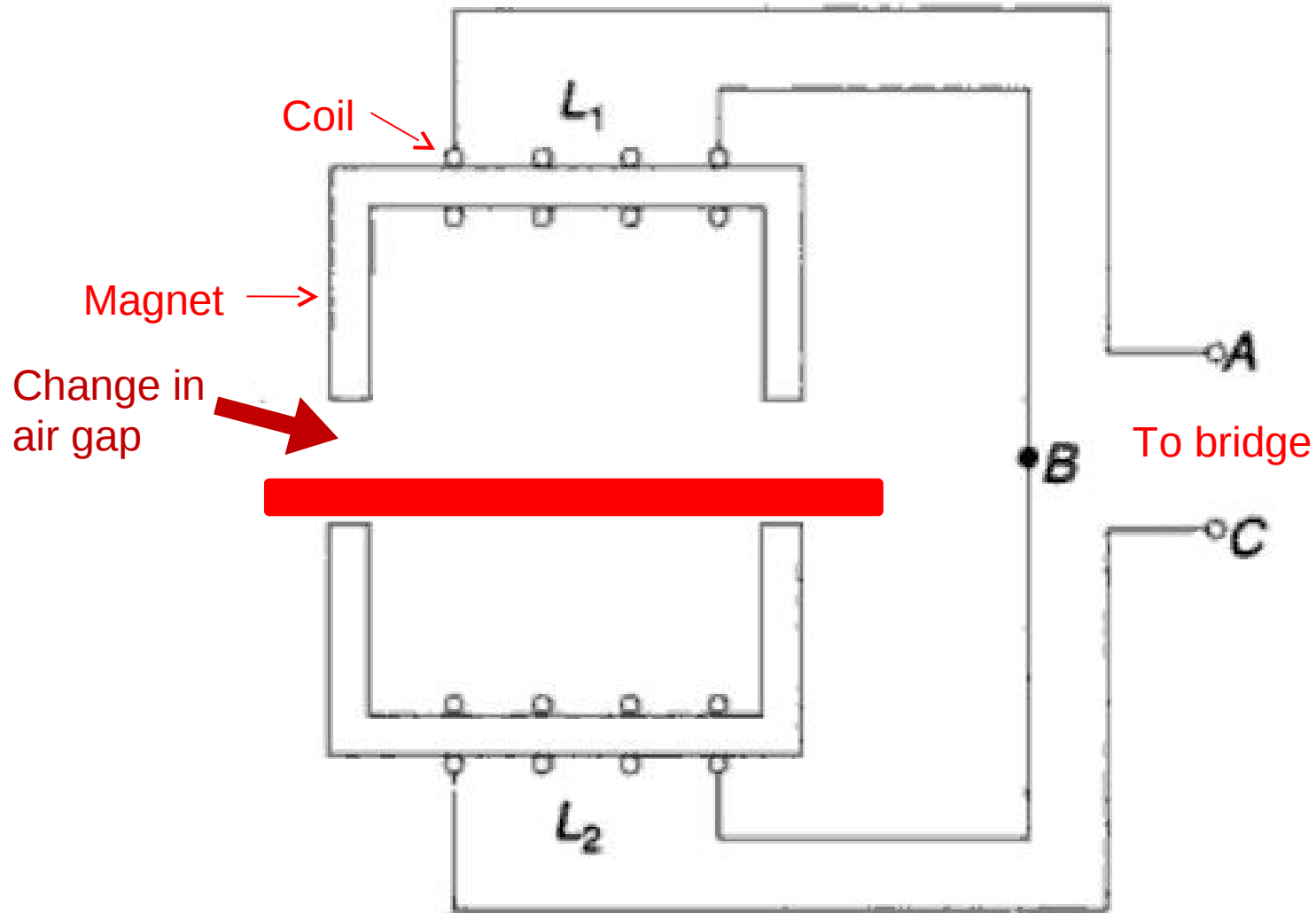


RELUCTANCE: the property of a magnetic circuit of opposing the passage of magnetic flux lines, equal to the ratio of the magnetomotive force to the magnetic flux

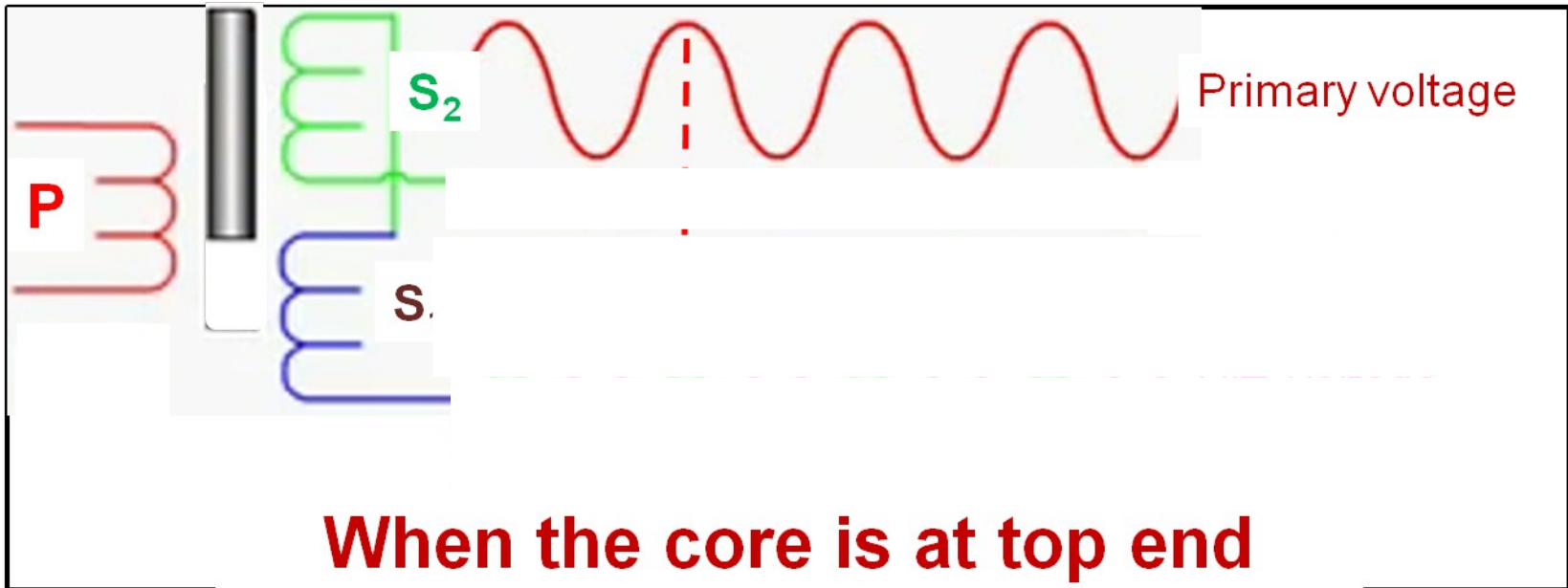
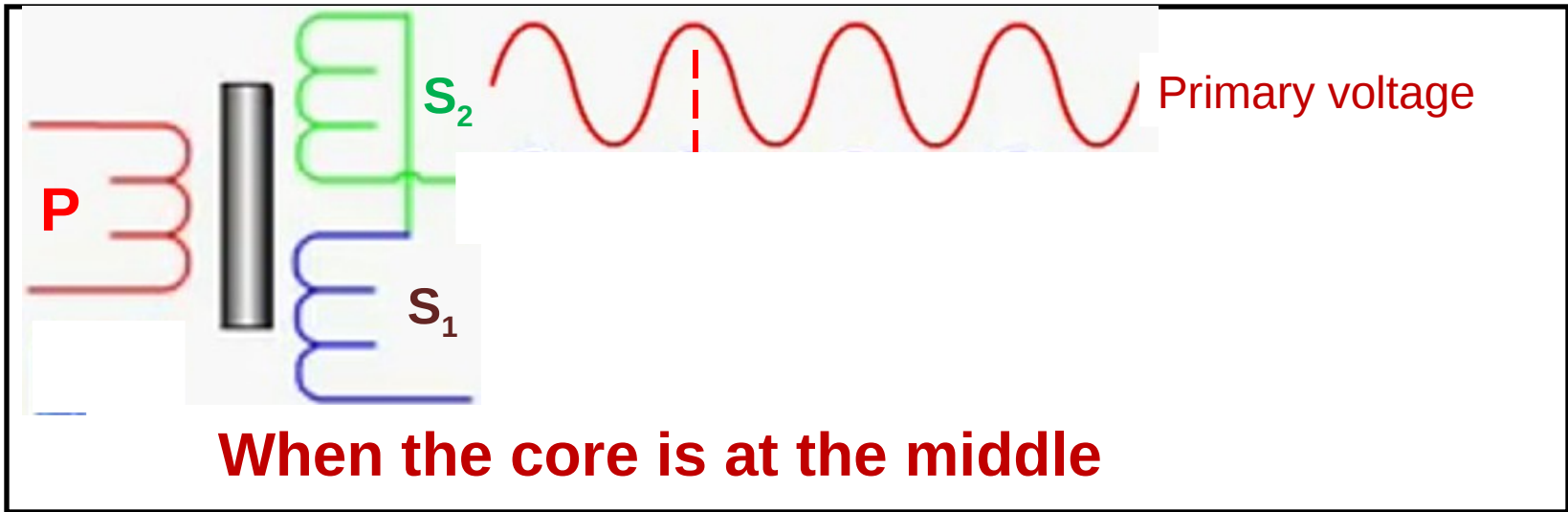
# Variable Inductance Type: Rotary Motion



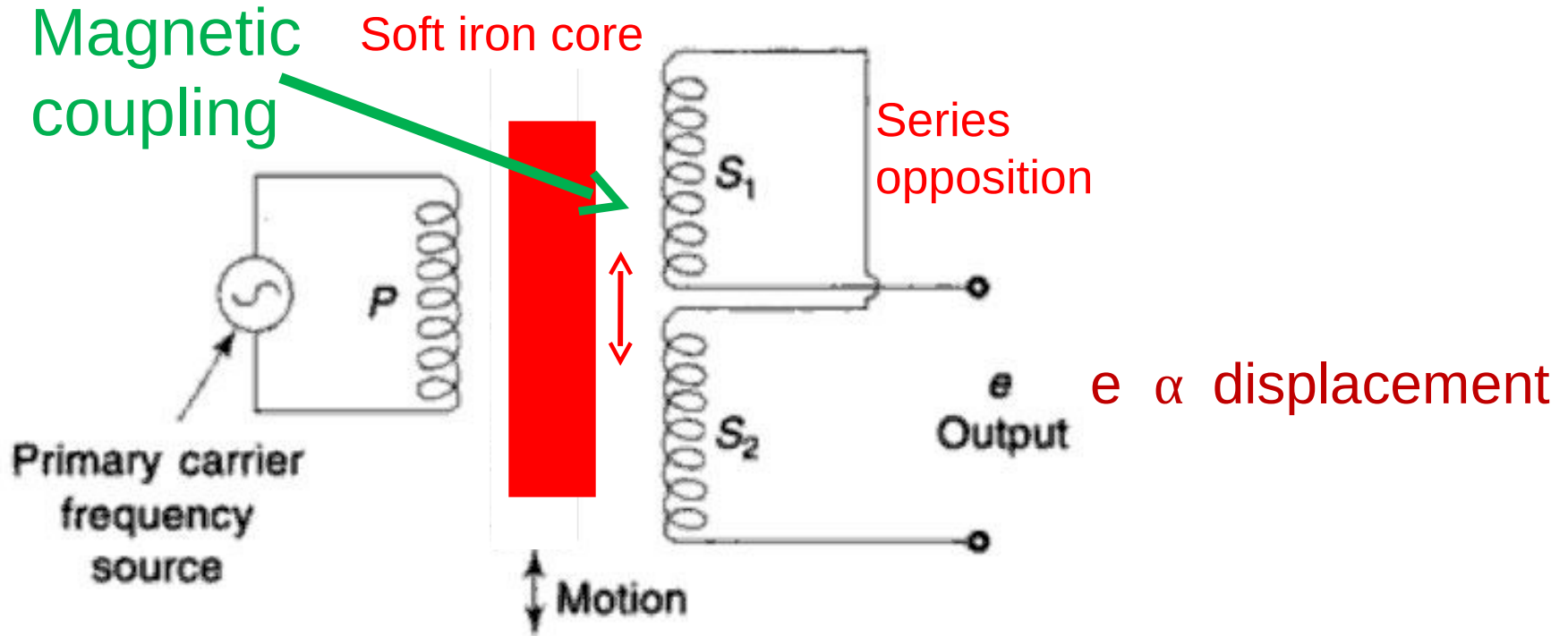
# Proximity Type: Variable Inductance



# LVDT : Linear Variable Diff. Transformer

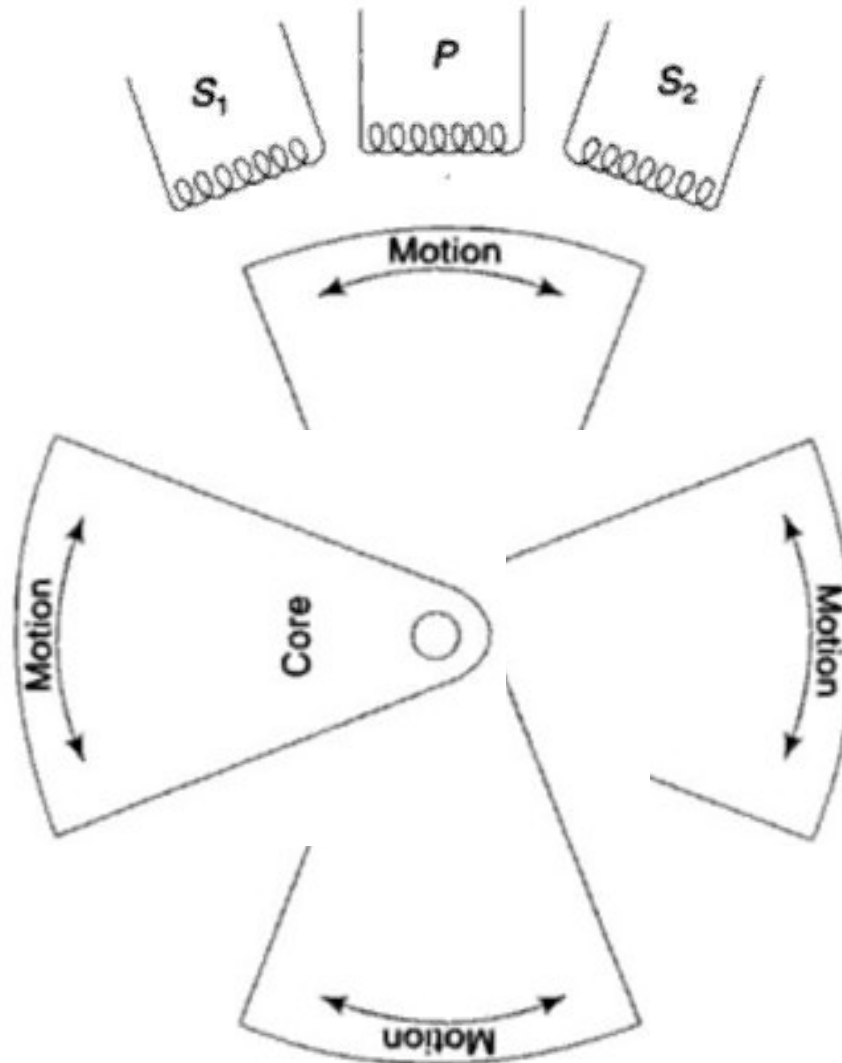


# LVDT : Linear Variable Diff. Transducer

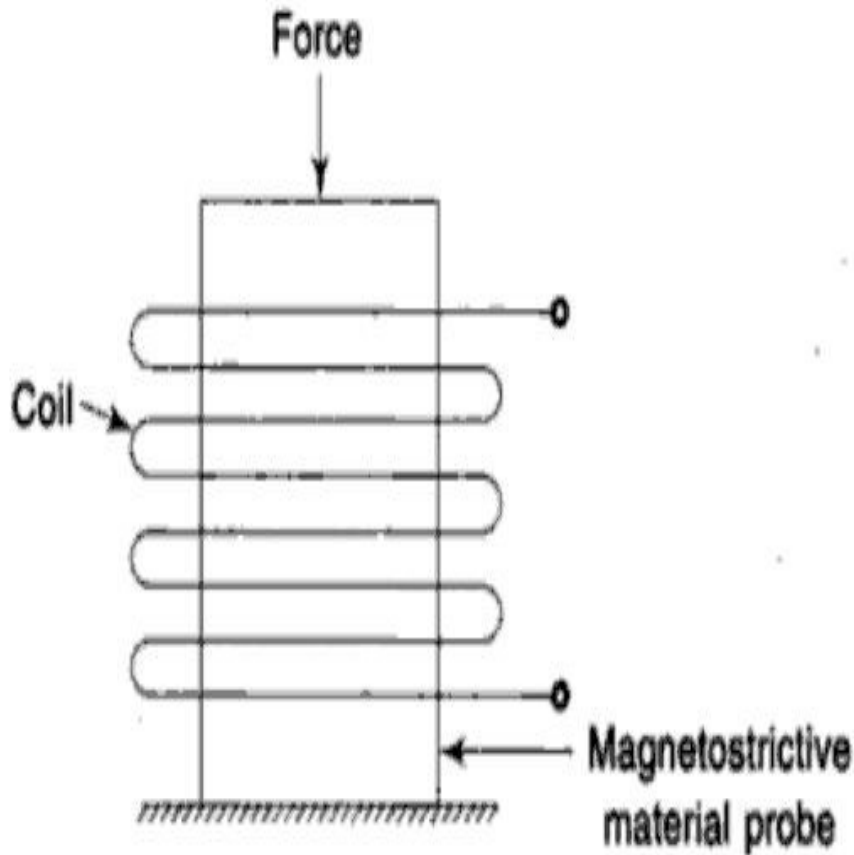


- Sensitive Transducer
- Linear over wide range

# LVDT : Linear Variable Diff. Transducer -ROTARY MOTION-



# Magnetostrictive Type



Principle: For ferromagnetic materials, Magnetic Permeability Changes with Mechanical Stress

For Ni it increases with compression And decreases with tension.

Hence L changes with compression or tension.

The magnitude and freq. of exciting current determines L.

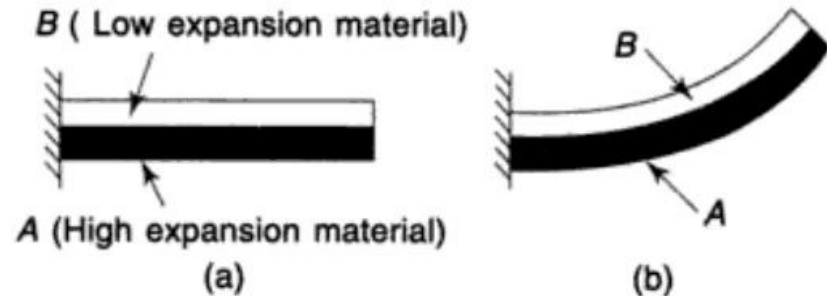
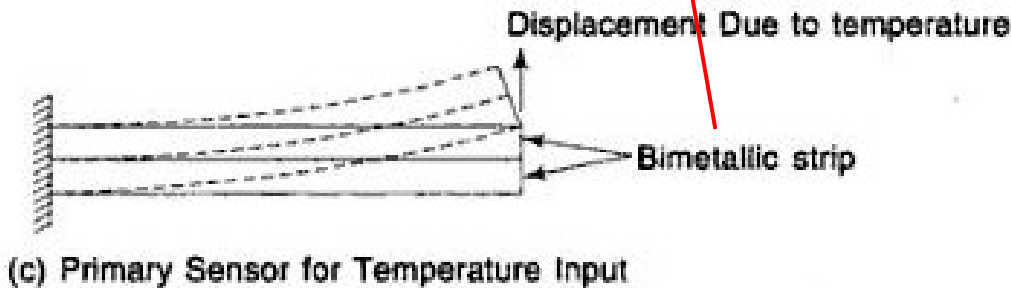
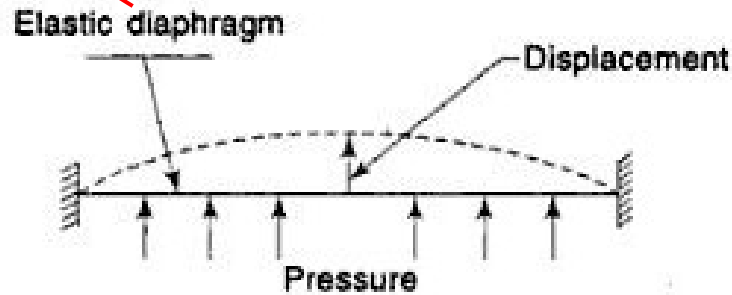
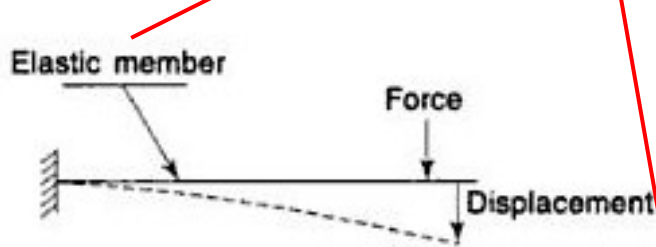
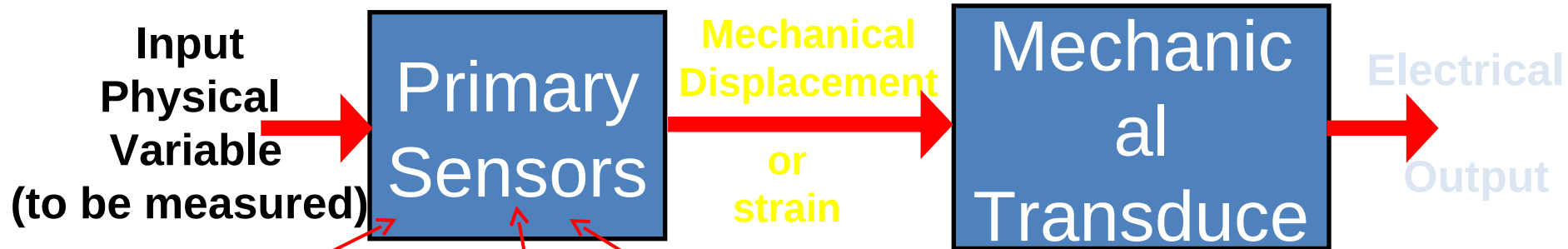
Force and motion can be measured.

Resonant freq. is high due to high mechanical impedance.

Since, physical properties of the material are changes individual calibration is Important.

# Electromechanical Transducers

## Primary Sensors for Displacements





# Capacitive Type Transducers

- It is a Displacement sensitive transducer

The capacitance **C** of a parallel plate capacitor is,

$$C = \frac{1}{3.6\pi} \epsilon \frac{A}{d}$$

**C** is capacitance,  $\mu\text{F}$

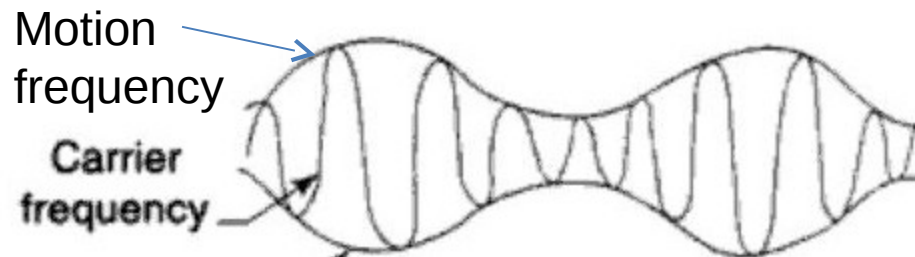
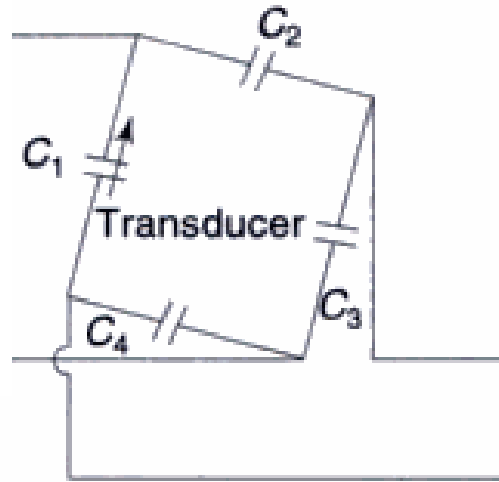
**A** is area of plates,  $\text{cm}^2$

**d** is distance between plates, cm

**$\epsilon$**  is dielectric constant of the medium

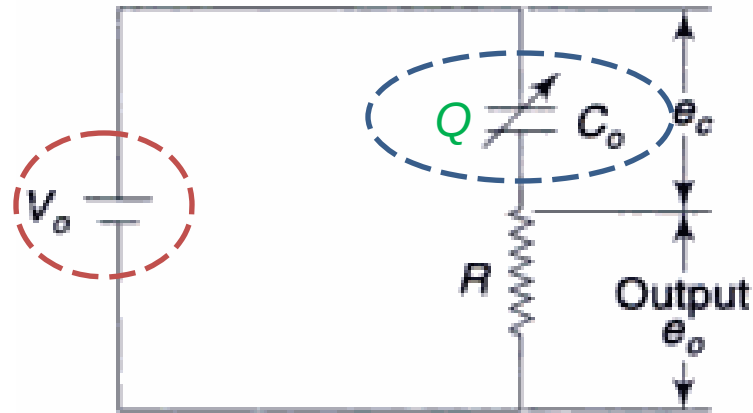
# Capacitive Type Transducers

Associated circuit for capacitive transducers



# Capacitive Type Transducers:

## DC Type: Only for Dynamic Measurements



$$V_0 = e_c + e_o \quad \dots\dots(1)$$

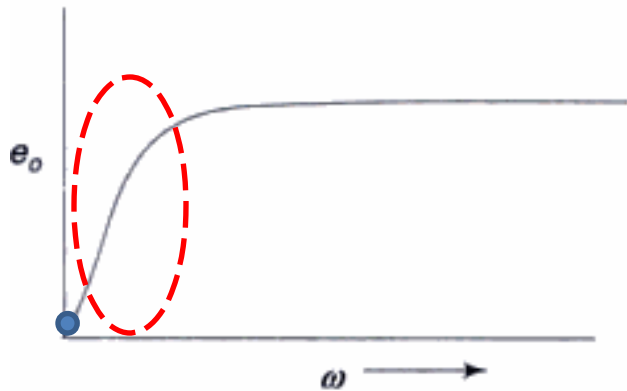
$$\text{and } Q = C_0 V_0 \quad \dots\dots(2)$$

$$\text{Also } e_o = V_0 - e_c \quad \dots\dots(3)$$

If motion is so fast that  $C_0$  changes to  $C$ , but  $Q$  remains almost unchanged, then

$$e_c = Q / C \quad \dots\dots(4)$$

$$\frac{e_o}{V_0} = \frac{C - C_0}{C} = \frac{\Delta C}{C} \quad (\text{prove})$$



Frequency response curve

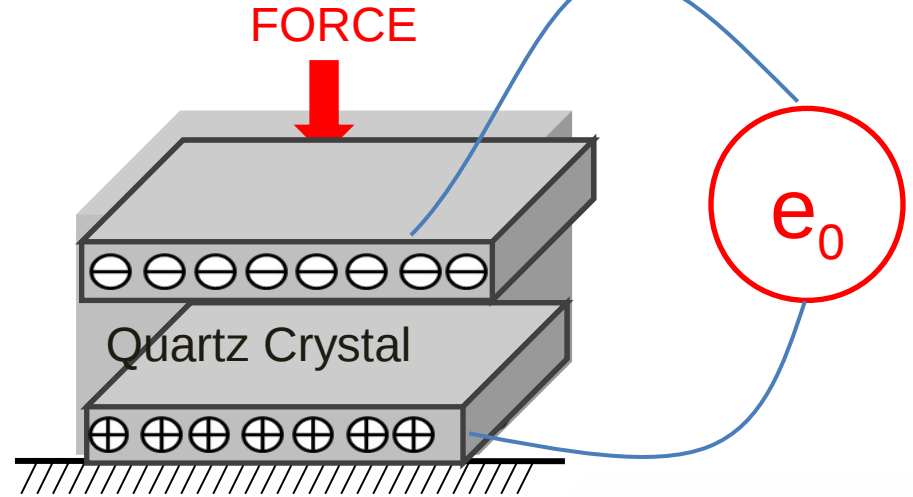
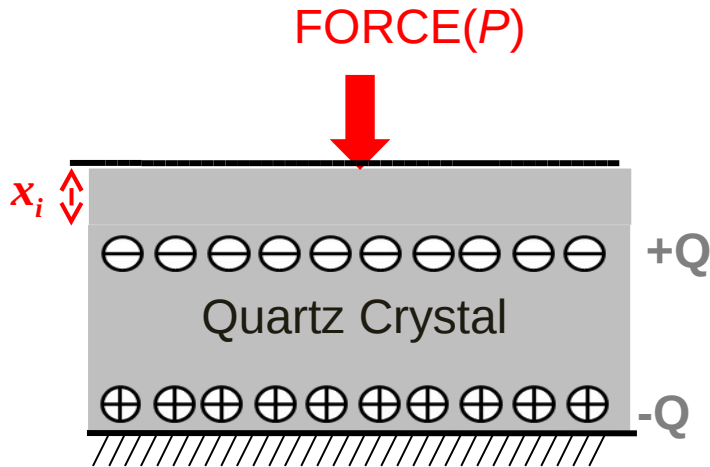
# Example 4.1

## Problem 4.1

A capacitive transducer consists of two plates of diameter 2 cm each, separated by an air gap of 0.25 mm. Find the displacement sensitivity.

*Solution*

# Piezo-electric Transducers: Piezoelectric Effect



$$Q \propto x_i$$

$$\text{i.e. } Q = K_1 x_i$$

$K_1$  is charge sensitivity constant

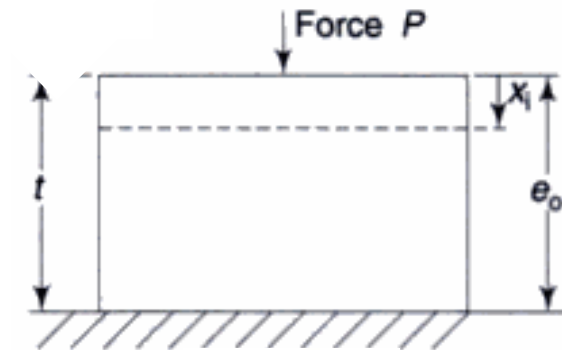
$$C = Q/e_0$$

$$\text{i.e. } e_0 = K_1 x_i / C$$

$$\text{i.e. } e_0 = K x_i$$

$K$  is voltage sensitivity constant

Parallel Plate Capacitor



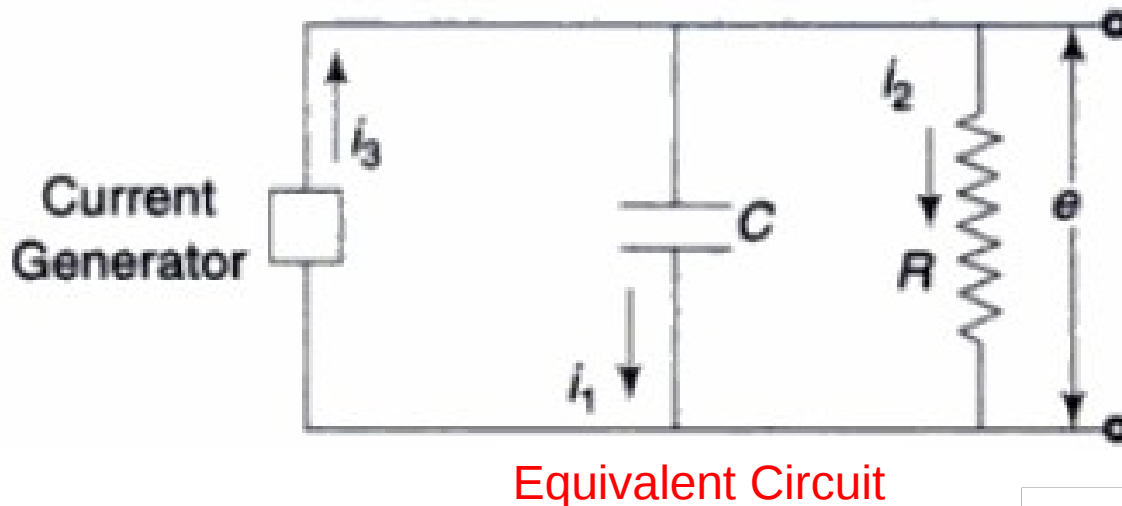
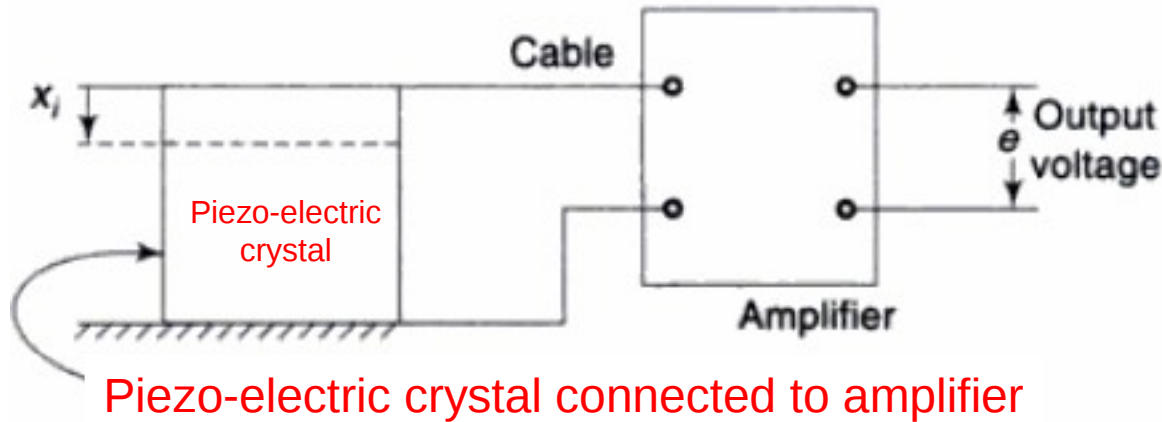
$$C = \frac{\epsilon A}{3.6\pi t} \mu f$$

$$C = \frac{\epsilon A}{1.31 \times 10^{11} t} \text{ farad}$$

$$P = EA \frac{x_i}{t}$$

$E$  is Young's modulus

# Dynamic Characteristic of Piezo-electric Transducers



Here  $C$  is the effective capacitance given by,

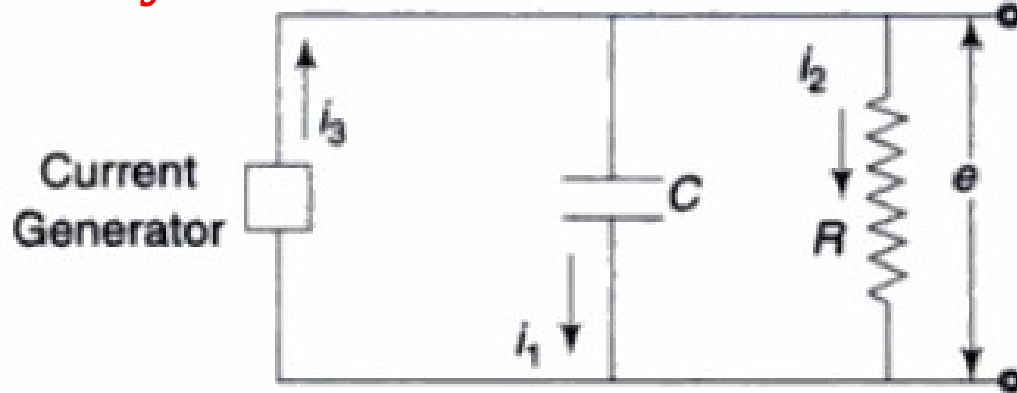
$$C = C_{crystal} + C_{cable} + C_{amplifier}$$

Also,  $R$  is effective resistance.

*Since  $R_{leak} \gg R_{amplifier}$*

$$R \approx R_{amplifier}$$

# Dynamic Characteristic of Piezo-electric Transducers



**KCL:**  $i_3 = i_1 + i_2$

$$i_3 = dQ/dt = dK_1 x_i / dt$$

$$= K_1 D x_i \quad \text{where } D = (d/dt)$$

$$i_2 = e / R$$

$$i_1 = C(de/dt) = CDe$$

**KCL:**  $K_1 D x_i = CDe + e/R$

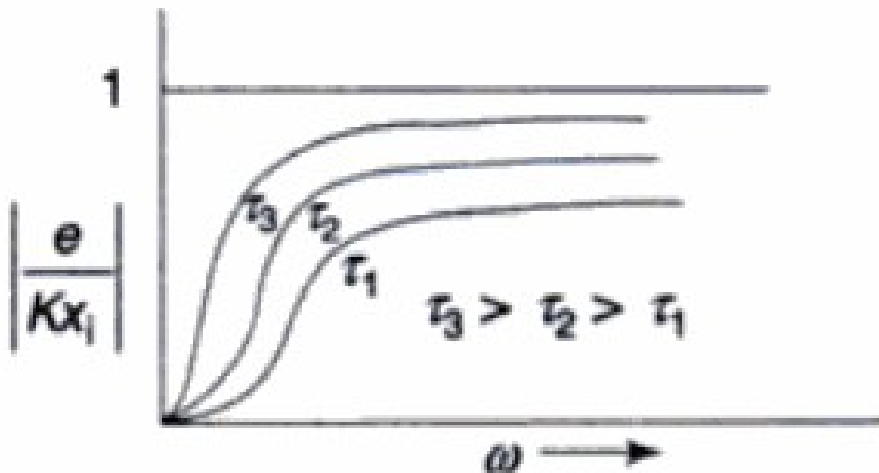
Using  $K = K_1/C$ ,  $(KC)Dx_i = CDe + e/R$

$$(KCR)Dx_i = RCDe + e$$

Let  $RC = \tau = \text{time constant of circuit}$ , then  $(K\tau)Dx_i = \tau De + e$

$$(K\tau)Dx_i = e(\tau D + 1)$$

If  $x_i = 0$ , ????



$$\left| \frac{e}{x_i} \right| = \frac{k\tau\omega}{\sqrt{1 + \tau^2\omega^2}}$$

$\tau$  should be large (upto a limit).

## Transient Response to Pulse Input

**Pulse:**  $x_i = A$  for  $0 < t \leq T$  and  $x_i = 0$ , for  $t > T$

For  $t > T$ , Putting  $x_i = 0$ , in  $(K\tau)Dx_i = e(\tau D + 1)$

we get,  $e(\tau D + 1) = 0$

**Solution:**  $e = Be^{-t/\tau}$  .....(1)

Where  $B$  is const. depending on initial condition.

For  $t = 0$ ,  $e = Be^{-0/\tau} = Be^0$

$e = B$  .....(2)

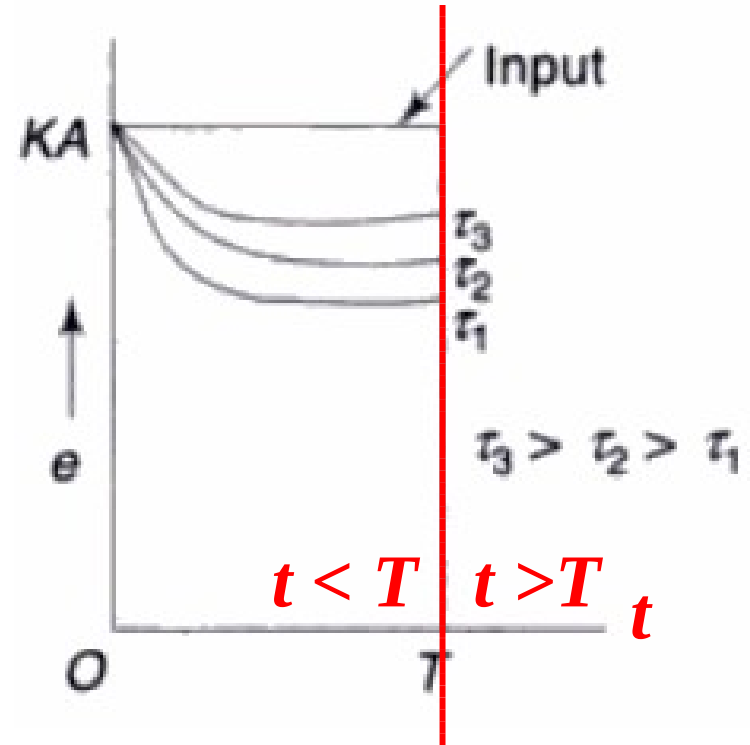
Also we have,  $e = Kx_i$ .

For  $t = 0$ ,  $x_i = A$  and so

$e = KA$  .....(3). From (2)&(3),

$B = KA$ . Hence (1) becomes  $e = KA e^{-t/\tau}$

It can be seen that shape of output pulse ( $e$ ) follows the **Shape of input ( $x_i$ )** for **larger value of  $\tau$** .





# Properties of some **Piezo-electric** Materials

<i>S.No.</i>	<i>Material</i>	<i>Charge sensitivity pC/N</i>	<i>Dielectric constant <math>\epsilon</math></i>	<i>Young's modulus N/m<sup>2</sup></i>
1.	Quartz	2.0	4.5	$9 \times 10^{10}$
2.	Tourmaline	1.9	6.6	$16 \times 10^{10}$
3.	Barium titanate	150	1380	$12 \times 10^{10}$
4.	Lead zirconate titanate	265	1500	$7.9 \times 10^{10}$

### Problem 4.3

A piezo-electric transducer has the following characteristics:

$$\text{Capacitance of crystal} = 10^{-9} \text{ F}$$

$$\text{Capacitance of cable} = 3 \times 10^{-10} \text{ F}$$

$$\text{Charge constant of crystal} = 4 \times 10^{-6} \text{ C/cm}$$

The oscilloscope used for read-out has a resistance of  $1 \text{ M}\Omega$  in parallel with a capacitance of  $10^{-10} \text{ F}$ . Find the amplitude of the output voltage, as displayed on the oscilloscope, if the crystal is subjected to a harmonic deformation of amplitude  $10^{-3} \text{ mm}$  and frequency  $200 \text{ Hz}$ .

$$R = 10^6 \Omega$$

$$C = 10^{-9} + 3 \times 10^{-10} + 10^{-10} \text{ F}$$
$$= 1.4 \times 10^{-9} \text{ F}$$

$$\tau = RC = 1.4 \times 10^{-3}$$

$$K_1 = 4 \times 10^{-6} \text{ coulomb/cm}$$

$$K = \frac{K_1}{C} = 2857 \text{ V/cm}$$

*We have,*

$$\left| \frac{e}{x_i} \right| = \frac{K\tau\omega}{\sqrt{1 + (\tau\omega)^2}}$$

$$\text{Putting } \omega = 2\pi \times 200$$

$$= 1256.6 \text{ rad/s ,}$$

$x_i = 10^{-4} \text{ cm}$  and other values in above relation we get,

$$e = 0.248 \text{ V}$$